# Nanocrystal quantum dots and quantum dot solids



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Soft Condensed Matter

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# Nanocrystal quantum dots and quantum dot solids

Nanocrystals and assemblies of nanocrystals: An overview

**Chemical preparation** 

**Electronic structure, optical and electrical properties** 

**Self-assembly of NC into solids** 

# 1.1 Clusters and nanocrystals

N<sub>x</sub>a



**cluster**: 1- 100 atoms Thermodynamic stability an structure depends on N:

Mono-disperse Au 55



#### Nanocrystal:

Thermodynamic stability is independent of N:

distribution in size and shape <sup>3</sup>



**Figure 3.** Ball and stick model of a Cd<sub>32</sub>S<sub>55</sub> molecule recently synthesized and structurally characterized by Herron and Wang.<sup>22</sup> The organic ligands are omitted for clarity. This molecule is a fragment of the CdS zinc blende lattice.

# **Colloidal nanocrystals**

#### CdSe: wurtzite



#### Nearly spherical shape, crystal facets

# 1.1 Colloidal nanocrystals

#### PbS: rock-salt structure







#### Nearly spherical shape, crystal facets



Different shapes of colloidal PbSe nanocrystals





Self-organization of non-spherical nanocrystals

### **First conclusions:**

Nanocrystals same crystal structure as big crystals

No thermodynamic selection of size and shape

Uniform size and shape can be obtained by "clever" chemistry (kinetics of growth)

# Nanocrystal quantum dots and quantum dot solids

Nanocrystals and assemblies of nanocrystals: An overview

**Chemical preparation** 

**Electronic structure, optical and electrical properties** 

### Three principles of making nanostructures

1

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Top-down: lithography >50 nm Fabrication in small numbers

Bottom-up (>1nm): Synthesis of molefraction numbers







### Three principles of making nanostructures

3 STM -manipulation: placing atom by atom (R. Feynman)

QuickTime<sup>™</sup> and a TIFF (Uncompressed) decompressor are needed to see this picture. Synthesis starting from molecular precursors "chemistry"

#### **Heterogeneous chemical preparation**



#### Chemical vapor deposition: ZnO epitaxial on saphire (Al<sub>2</sub>O<sub>3</sub>)





#### **Heterogeneous chemical preparation**

Metal-catalysed deposition: Vapor-Liquid-Solid method



Lieber, Adv. Mater. 12, 298 (2000); Bakkers, Nature Materials 3, 769 (2004)

# Homogeneous chemical preparation: colloidal suspensions

Solutes  $\Leftrightarrow$  solid

Solutes ⇔ nanocrystal suspension ⇔ solid



Homogeneous chemical preparation: colloidal suspensions

#### Synthesis in aqueous solution

 $Cd(CIO_4)_2$  in water +  $H_2S$  (gas) + surfactant:  $Na(PO_3)_n$ 

### **Organo-metallic synthesis at high temperature** $Cd(CH_3)_2 + TOP-Se$ in **TOP-TOPO-HDA** nucleation - growth + surface annealing

C. B. Murray, JACS 115, 8706 (1993)

1500 citations!



#### Homogeneous chemical preparation: colloidal suspensions



#### PHYSICO-CHEMICAL EVALUATION: TEMPORAL SEPARATION OF NUCLEATION AND GROWTH

Debye (1949): quantitative formation of critical nuclei starting from a critical monomer concentration (micelles)

 $c \text{ Cd-TOPO} + c \text{ Se-TOP} \Leftrightarrow (\text{CdSe})_c \text{TOPO}_m + (c-m)\text{TOPO} + c \text{ TOP}$ 



21

# 2.3 Surface chemistry

#### **Organic surfactant molecules**

strong influence on kinetics of growth

stabilise colloidal dispersion how?

prevent chemical surface reactions with H<sub>2</sub>O, O<sub>2</sub>

passivate electronic surface states



## 2.3 Surface chemistry

#### **Inorganic surface molecules**



**Summary:** 

**Three principles of fabrication** 

**Chemical synthesis** 

-deposition on substrate

- nucleation and growth in solution: colloidal nanocrystals

- colloidal nanocrystals are ideal building blocks for new "supercrystals"

# 3 Electronic properties of nanocrystalline quantum dots

3.1 Energy levels: a qualitative understanding
3.2 Energy levels: More sophisticated models
3.3 Charge (and spin) interactions
3.4 Comparison with experimental results

# What do you know about the electronic structure of solids?

### **Potential wells**



### atom nanocrystal artificial atom

## **3.1 One electron in empty box**



**Excess electrons** in an insulating nanocrystal: bound conduction states **Excess holes** : valence states

\*\*\*\*\*

Size ↓

**S** LUMO

#### One electron in a box filled with crystal lattice



Bloch function  $U_k$  determines band structure of macroscopic crystal and forms the basis for the energy levels in a nanocrystal

### One electron in a box filled with crystal lattice



**Free electron** 

Electron – lattice scattering (bands) Quantumconfinement

### 3.2 More sophisticated models: Tight-binding



**Linear Combination of Atomic Orbitals** 

#### CAN WE PROBE THE ELECTRONIC STRUCTURE ?

#### **Optical spectroscopies**

Transition between two levels (creation - annihilation of an electron and hole)

#### **Resonant tunneling spectroscopy**

Single level in QD involved

Selection rules

Limited spatial resolution

k - selection rules do not play a role : density of states can be probed

Atom-scale spatial resolution



### 3.4 Light absorption - luminescence





Discrete inter-band transitions Selection rules: Bloch part Inhomogeneous line-broadening Quantum confinement Photoluminescence quantum yield

### 3.4 bright luminescence - strongly sizedependent: applications?



### **Resonant Tunneling**




# 3.4 shell-tunneling of 3.5 nm CdSe



## **Summary: Electronic structure**

- Quantum confinement: discrete energy levels determined by the nature and size of crystal
- **Ensemble optical spectroscopy**
- Optical and electrical spectroscopy on single Nan crystal possible

## SECTION 5: SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

Chemical synthesis of MPNC is an interesting topic on itself (see Mastercourse TOPICS IN NANOSCIENCE)



Electron-conducting quantum dot solids: novel materials based on colloidal semiconductor nanocrystals Vanmaekelbergh and P. Liljeroth*Chemical Society Reviews* 34, 299-312 (2005) and references in there

From the viewpoint of self-assembly:

Building blocks have dimensions one order of magnitude larger than molecules, much smaller than the "usual" colloids (> 100 nm)

"Spherical" building blocks have a simple geometry (on the first sight!), there are often considered as "large atoms"....but...the crystal facets, and the organization of capping molecules around the nanocrystal provide new degrees of freedom and lead to new phenomena



Small is different. U. Landman, Faraday Discuss. 125, 1 (2004)

From the viewpoint of self-assembly:

Non-spherical building blocks lead to new degrees of freedom and new disorder effects with respect to an ordinary atomic solid



Strength of bonding between building blocks (pair potential) is not directly related to the electronic coupling unlike for ordinary atoms

Pressure/temperature phase diagrams and superlattices of organically functionalised metal nanocrystal monolayers. J. R. Heath et al., JPC B 101, 189 (1997).



#### Importance for nanophysics and material science:

Nanocrystals are metallic, magnetic, semiconductor compounds with size - tunable properties

- Electron (hole) wave confinement
- **Dielectric confinement**

Volume-dependent magnetic moment (particle-size smaller than magnetic domain)



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SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS INTRODUCTION: WHY IS THIS INTERESTING?

Importance for nanophysics and material science:

Solids of "artificial atoms" can be prepared; the electronic properties of these "artificial solids" compared to ordinary atomic solids are of huge interest for physical sciences.

Examples: dipolar (Förster) energy transfer, exchange energy transfer, distance-dependent electronic coupling, metal-insulator transitions...



#### Applications: Materials with novel opto-electrical and magnetic functions that depend on the nature of the building block and the interactions between them in the condensed phase

Electron-conducting quantum dot solids: novel materials based on colloidal semiconductor nanocrystals Vanmaekelbergh and P. Liljeroth*Chemical Society Reviews* 34, 299-312 (2005) and references in there



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SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS SUPERLATTICES FORMED BY **DESTABILIZATION** OF A NANOCRYSTAL COLLOIDAL SOLUTION

<u>Principle</u>: "destabilization" means increasing the chemical potential of the nanocrystal building blocks in the solution. In such a way a spontaneous assembly can occur until equilibrium between the solution and the solid is reached



Two methods of destabilization:

$$\mu = \mu^o + kT \ln \frac{c}{c^{\text{Re}f}}$$

•increasing the concentration of NC by thermal evaporation of solvent

- •Increasing external pressure (Langmuir-Blodgett trough)
- addition of a non-solvent to a colloidal solution
- other methods? Why is T-increase not working?

## 3-D system

Gas-pressure (exerted by molecules on the walls of container)

$$p = -\left(\frac{\partial F}{\partial V}\right)_{T,N} = -\left(\frac{\partial U}{\partial V}\right)_{T,N} + T\left(\frac{\partial S}{\partial V}\right)_{T,N}$$

## 2-D system

Surface-pressure - excerted by units of assembly on the edges of the system

$$\pi = -\left(\frac{\partial F}{\partial A}\right)_{T,N} = -\left(\frac{\partial U}{\partial A}\right)_{T,N} + T\left(\frac{\partial S}{\partial A}\right)_{T,N}$$

Surface-tension: change of free energy with change of area

$$\gamma = \left(\frac{\partial F}{\partial A}\right)_{T,N} = -\pi$$

In a Langmuir-trough the "surface pressure" [ $\gamma$ (water)- $\gamma$ (particles)] is measured by pulling on a Welhelminiplate; the meaning of this result is thus  $\pi$ (particles)- $\pi$ (pure water) (pure water is the reference)

Molecular driving forces. Ken A. Dill and S. Bromberg, ISBN 0-8153-2051-5 Intermolecular & Surface Forces. J. Israelachvili. ISBN 0-12-375181-0

#### ASSEMBLY IN A LANGMUIR-BLODGETT TROUGH



## Geometry of am MP NC:

Excess volume: (Volume of cone = volume available for ligand) determined by footprint (f) of ligand on surface, radius (R) of NC and length L of Molecule:  $V_e$  scales with L<sup>3</sup>/R<sup>2</sup>

### (p,A) Phase diagram and structure

The phase behavior and structure of twodimensional MPNC layers must be determined by entropy effects and by dispersion interactions between capping molecules and between NC cores. The geometry of the MPNC building blocks is essential, especially L vs. R and V<sub>e</sub> determine phase behavior and structure

QuickTime<sup>™</sup> and a TIFF (LZW) decompressor are needed to see this picture.

<u>Case I:</u>  $V_e > 350 \text{ Å}^3$ <u>Case II:</u> 150  $\text{Å}^3 < V_e < 350 \text{ Å}^3$ <u>Case III:</u>  $V_e = 30 \text{ Å}^3$ 

#### nanocrystals have facets - effect on ordering of molecules!

Pressure/temperature phase diagrams and superlattices of organically functionalised metal nanocrystal monolayers. J. R. Heath et al., JPC B 101, 189 (1997).

SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

ASSEMBLY IN A LANGMUIR-BLODGETT TROUGH



estimated number of crystallites applied onto the water surface.

SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

ASSEMBLY IN A LANGMUIR-BLODGETT TROUGH



#### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS ASSEMBLY IN A LANGMUIR-BLODGETT TROUGH





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SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

ASSEMBLY IN A LANGMUIR-BLODGETT TROUGH

<u>Case I:</u>  $V_e > 350 \text{ Å}^3$  London forces between capping molecules are dominant, leading to low density phases with order and decreasing disorder at higher densities

**d**π/**dT**<**0** QuickTime™ and a TIFF (LZW) decompressor are needed to see this picture. QuickTime<sup>™</sup> and a QuickTime<sup>™</sup> and a TIFF (LZW) decompressor TIFF (LZW) decompressor are needed to see this picture. are needed to see this picture. QuickTime™ and a TIFF (LZW) decompressor are needed to see this picture.

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ASSEMBLY IN A LANGMUIR-BLODGETT TROUGH

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$$\frac{\partial \pi}{\partial T} = \frac{\partial S}{\partial A}$$

## Normally positive, but here negative!

Pressure/temperature phase diagrams and superlattices of organically functionalised metal nanocrystal monolayers. J. R. Heath et al., JPC B 101, 189 (1997).

QuickTime<sup>™</sup> and a TIFF (LZW) decompressor are needed to see this picture. SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

3-D SUPERLATTICES FORMED BY DESTABILIZATION OF A NANOCRYSTAL COLLOIDAL SOLUTION

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- \*\*\* other methods? Why is T-increase not working?

Homogeneous nucleation: formation of 3-D micrometer large supperlattices

<u>Heterogeneous nucleation on a substrate</u>: formation of 2-D monolayers, bilayers etc. by dropcasting and thermal evaporation

E. V. Shevchenko et al., J. Am. Chem. Soc. 124, 11480 (2002),

C. B. Murray et al., Science 270, 1335 (1995); IBM J. RES. & DEV. 45, 47 (2001)

AL. Rogach et al. Adv. Funct. Mater. 12, 654 (2002)

SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS THERMODYNAMICS AND MOLECULAR DYNAMICS



Small is different. U. Landman, Faraday Discuss. 125, 1 (2004)

Reduce V - Calculate P and U

Free energy can be calculated from:

$$p = -\left(\frac{\partial F}{\partial V}\right)_{T,N}$$

From F and U, -TS can be calculated (increase of entropy due to reduction of volume)

#### MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: Case of CdSe

### L/R is important part of the code



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Small is different. U. Landman, Faraday Discuss. 125, 1 (2004)

### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS HOMOGENEOUS NUCLEATION AND GROWTH BY SOLVENT EVAPORATION: CASE OF CdSe

"First" example was the formation of three-dimensional 5 to 50 micrometer colloidal crystals of CdSe





Fig. 12. TEM images of 3D arrangements of  $CoPt_3$  (a) and CdSe (b) nanocrystals, and HRTEM images of (100) (c) and (110) (d) projections along the CdSe superlattice with corresponding FFTs.



Small angle XRD spectra: structure of superlattice of NC building blocks

Wide-angle XRD spectra: atomic structure of nanocrystal and nanocrystal orientation in superlattice

2 Derivation of the Bragg equation  $2d \sin \theta = n\lambda$ ; here *d* is the spacing of parallel atomic and  $2\pi n$  is the difference in phase between reflections from successive planes. The reflecting have nothing to do with the surface planes bounding the particular specimen.

Small angle XRD spectra: structure of superlattice of NC building blocks

Wide-angle XRD spectra: atomic structure of nanocrystal and nanocrystal orientation in superlattice



C. B. Murray et al., Science 270, 1335 (1995); IBM J. RES. & DEV. 45, 47 (2001)

#### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

#### HOMOGENEOUS NUCLEATION AND GROWTH BY ADDITION OF NON-SOLVENT





AL. Rogach et al. Adv. Funct. Mater. <u>12</u>, 654 (2002)

E. V. Shevchenko et al., J. Am. Chem. Soc. 124, 11480 (2002),

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### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: Case of CdSe



## Subtle effects of secret parts of the "code" Is it the crystal dipole moment?

C. B. Murray et al., Science 270, 1335 (1995); IBM J. RES. & DEV. 45, 47 (2001)

AL. Rogach et al. Adv. Funct. Mater. 12, 654 (2002)

#### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS HETEROGENEOUS NUCLEATION AND LAYER FORMATION



SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: Case of PbSe

**AFM: orientation due to HOPG substrate?** 

## STM and spectroscopy 1.00 0.75 (V/An) Vb/lb 0.50-0.25-0.00-0.0 -0.5 0.5 $V_{\rm bias}\,({\sf V})$

1.0

#### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: Case of PbSe

### STM and spectroscopy





#### MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: Case of PbSe



#### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS

MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: bimodal layers of gold

If size ratio is far from suitable, nanocrystals do not mix!





Gold nanocrystals with size ratio between 0.48 and 0.63 leads to  $AB_2$  structures



Gold nanocystal with size ratio between 0.24 and 0.48 leads to AB structures

Kiely, Nature 396, 444 (1998) J. V. Sanders, M. J. Murray, Nature 275, 201 (1978)

#### SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: binary layers of FePt + CdSe


The code in parameters: L/R, excess volume, ...



Small is different. U. Landman, Faraday Discuss. 125, 1 (2004)

## SELF-ASSEMBLY OF MONOLAYER-PROTECTED NANOCRYSTALS MONO, BI, TRI LAYERS BY DROPCASTING AND SOLVENT EVAPORATION: binary layers of FePt + CdSe



Disordered layers form if solvent evaporates to fast

